

IM2 - 1.1 (P - aV1) Rational Exponents & Radicals Explained

N.RN.1

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Directions - (N.RN.1) Given the following expressions, expand the base, simplify the expression, and explain the simplification.

1. Original = Expanded = Simplified

$$\sqrt[3]{512} = 512^{\frac{1}{3}} = (\underbrace{8 \cdot 8 \cdot 8}_{2})^{\frac{1}{3}} = \underline{8 \cdot 8} = 8^2 = \boxed{64}$$

Explanation: The simplified expression is 2 of the 3 repeated factors of the product 512.

$$256^{\frac{1}{4}} = (\underbrace{4 \cdot 4 \cdot 4 \cdot 4}_{1})^{\frac{1}{4}} = \underline{4} = \boxed{4}$$

Explanation: The simplified expression is 1 of 4 repeated factors of the product of 256.

$$81^{\frac{3}{4}} = (\underbrace{3 \cdot 3 \cdot 3 \cdot 3}_{3})^{\frac{3}{4}} = \underline{3^2} = \boxed{27}$$

Explanation: The simplified expression is 3 out of 4 repeated factors of the product of 81.

$$3125^{\frac{2}{5}} = (\underbrace{5 \cdot 5 \cdot 5 \cdot 5 \cdot 5}_{2})^{\frac{2}{5}} = \underline{5^2} = \boxed{25}$$

Explanation: The simplified expression is 2 out of 5 repeated factors of the product of 3125.

Directions - (N.RN.1) Explain why the two expressions are equivalent, showing the steps for simplification.

Example: $\sqrt[6]{4^3} = (\sqrt[6]{4})^3$
 $\sqrt[6]{64} = (1.2599)^3 \leftarrow$ Calculator used for the 6th root of 4
 $2 = 2$

1st Exp 1st Root

5. $\sqrt[4]{16^2} = (\sqrt[4]{16})^2$
 $\sqrt[4]{256} = (2)^2$
 $4 = 4 \quad \checkmark$

6. $\sqrt[3]{27^4} = (\sqrt[3]{27})^4$
 $\sqrt[3]{531441} = (3)^4$
 $81 = 81 \quad \checkmark$

7. $\sqrt[3]{8^3} = (\sqrt[3]{8})^3 = 8^{\frac{3}{3}} = 8^1 = 8$
 $\sqrt[3]{512} = (2)^3$
 $8 = 8 \quad \checkmark$

8. $\sqrt{9^3} = (\sqrt{9})^3$
 $\sqrt{729} = (3)^3$
 $27 = 27 \quad \checkmark$

9. $\sqrt[3]{216^2} = (\sqrt[3]{216})^2$
 $\sqrt[3]{46656} = (6)^2$
 $36 = 36 \quad \checkmark$